



CAUSAL STRUCTURE OF
BLACK HOLE EVAPORATION.

Joe Schindler

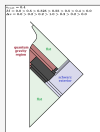
UCSC Physics

November 2016

Goal:

Show this diagram

(true penrose diagram for bh formation and evaporation)

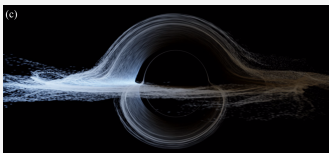


and convince you that you care.

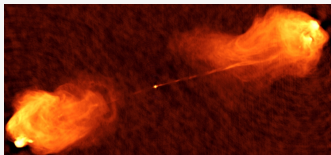
Step 1:
Context

WHAT IS A BLACK HOLE?

Astrophysical black holes.

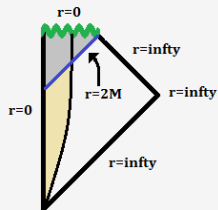
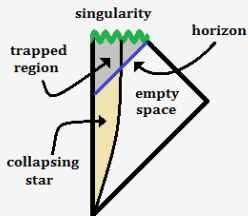


(Gargantua, Thorne 2015)



(Cyg A, NRAO via Narayan 2015)

Theoretical black hole spacetimes.

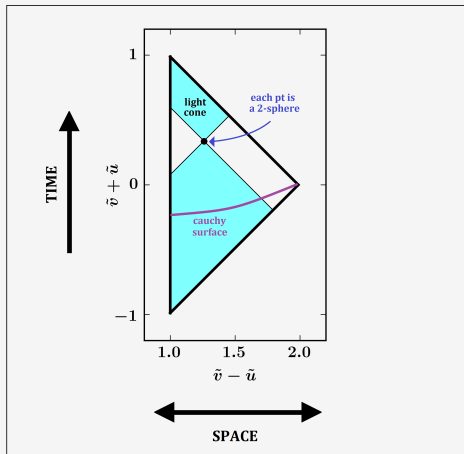


Key feature: Trapped region leading to extreme curvature.

PENROSE DIAGRAMS.

Visualizing a spacetime:

Penrose Diagram = GOOD



EVERYTHING YOU NEED TO KNOW ABOUT GR.

► **spacetime** = manifold (w/ one timelike dimension)

► **metric** ($g_{\mu\nu}$) encodes geometry:

$ds^2 = dx^2 + dy^2$ (flat plane)	$ds^2 = R^2 (d\theta^2 + \sin^2 \theta d\phi^2)$ (sphere)	$ds^2 = -dt^2 + dr^2 + r^2 d\Omega^2$ (flat spacetime)
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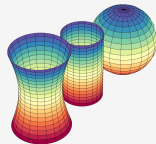
► **lightcones** determine causal structure

► **gravity** from coupled matter+metric eqns:

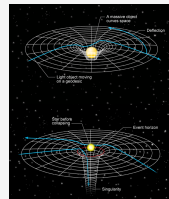
$$S = S_{\text{grav}} + S_{\text{matter}}$$

► **curvature** relates to matter content, partly through $G_{ab} = 8\pi T_{ab}$.

$$\begin{array}{lclcl} \text{total curvature} & = & \text{ricci part} & + & \text{traceless part} \\ (R_{abcd}) & \rightarrow & (G_{ab}) & , & (C_{abcd}) \end{array}$$



(Wikimedia Commons)



(Nastase 2009)

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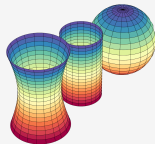
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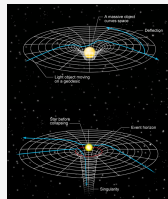
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(flat plane)

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(sphere)

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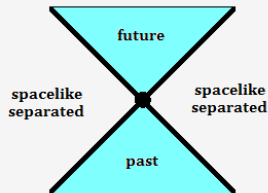
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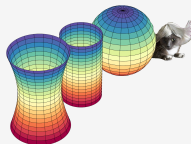
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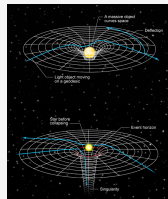
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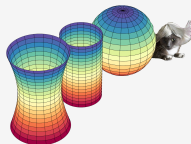
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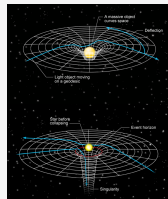
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local
matter

waves and
distant sources



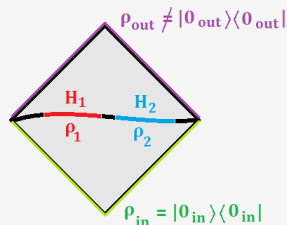
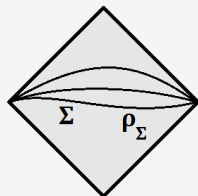
(Wikimedia Commons)



(Nastase 2009)

QFT IN CS.

- ▶ **density matrix**, pure states, mixed states
- ▶ each **cauchy surface** has a density matrix on its **hilbert space**
- ▶ HS is tensor product of local DOFs
- ▶ definition of **particles/vacuum not unique**
- ▶ classical wave basis \Leftrightarrow fock basis
- ▶ semi-classical limit from $\langle T_{\mu\nu} \rangle$
- ▶ locally flat \Rightarrow locally standard QFT

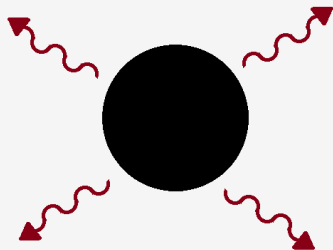


Step 2:
Motivation

MOTIVATION.

black holes evaporate by emitting (approximately) thermal radiation

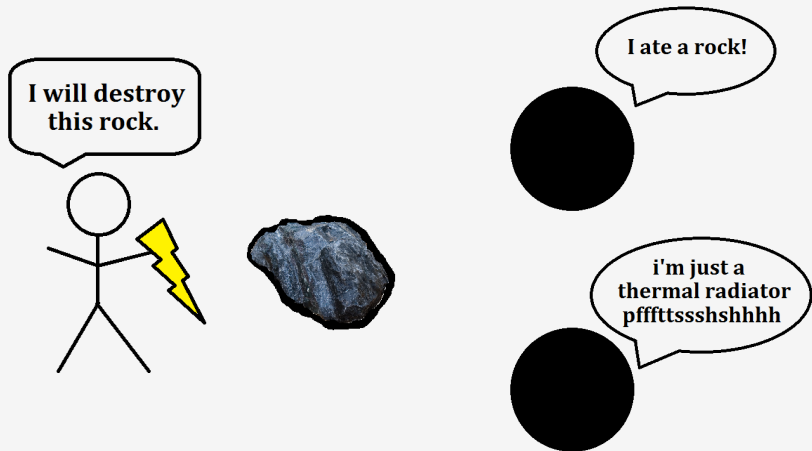
$$(T \propto 1/M)$$



stuff goes in \Rightarrow hawking radiation comes out

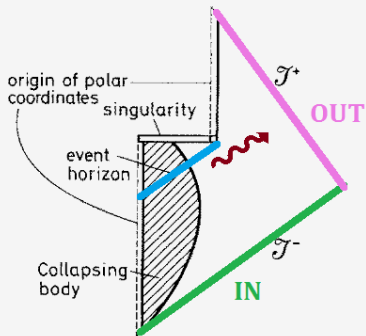
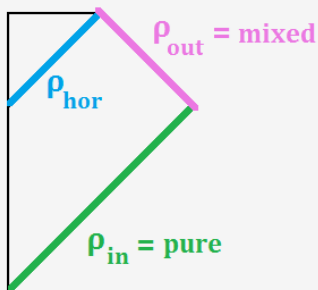
MOTIVATION.

- ▶ “information paradox”?



MOTIVATION.

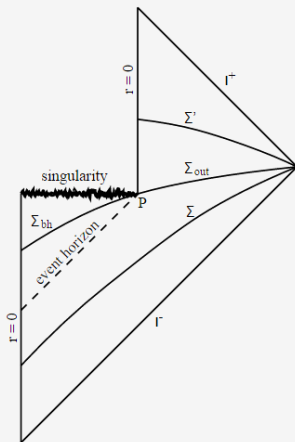
- ▶ not well posed



(Hawking 1975 + annotation)

MOTIVATION.

- ▶ doesn't correspond to any spacetime
- ▶ no cauchy surface
- ▶ everything happens at the bad point (P)
- ▶ singularity?
- ▶ general: no fake diagram contains any unknown information
- ▶ conclusion: not very useful (or worse!)
- ▶ goal: explicitly construct evaporating bh spacetime and compute diagram



(1993)

Step 3:

Explicitly Computed Penrose
Diagrams

ALGORITHM.

New algorithm computes any diagram of the form

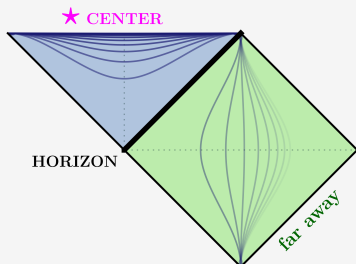
$$ds^2 = -f(r) dt^2 + f(r)^{-1} dr^2 + r^2 d\Omega^2 .$$

(*Mink, Schwarz, R-N, dS, AdS, Ax-Kerr-Newm, Hayward, S-dS, S-AdS, ...*)

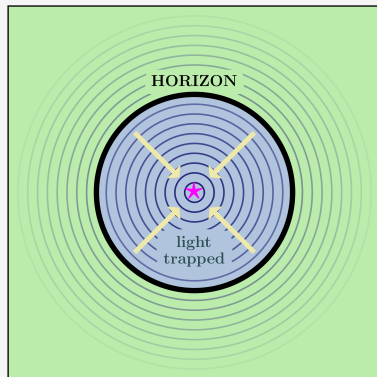
- ▶ numerically computable with any number of horizons
- ▶ metric analytic across horizons
- ▶ slightly expands class of known diagrams

SCHWARZSCHILD BH.

penrose diagram



coordinate "time" slice



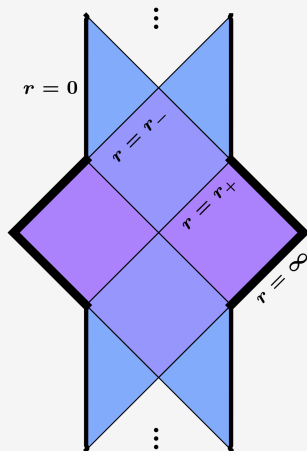
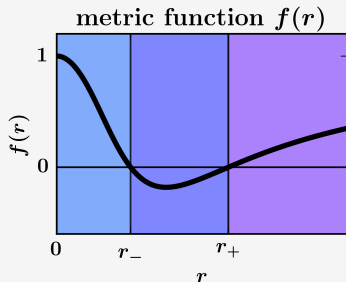
"schwarzschild radius" $R = \frac{2GM}{c^2}$

STRONGLY SPHERICALLY SYMMETRIC SPACETIMES.

- ▶ **function $f(r)$ specifies metric**

$$ds^2 = -f(r) dt^2 + f(r)^{-1} dr^2 + r^2 d\Omega^2$$

- ▶ **horizons** where $f = 0$
- ▶ **maximal extension** vs. collapse/evap

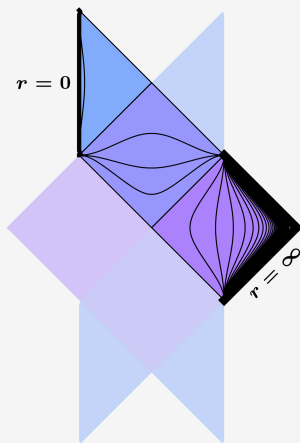
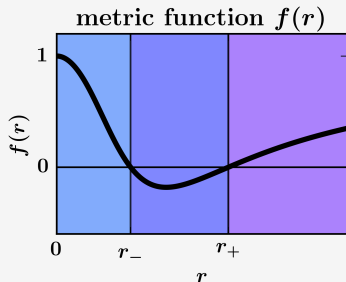


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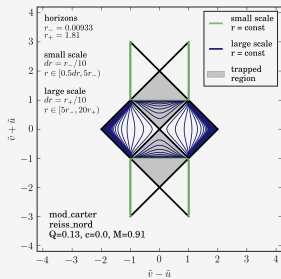
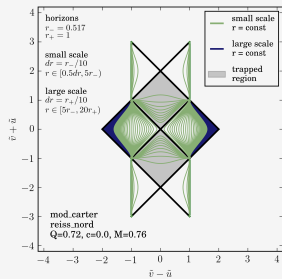
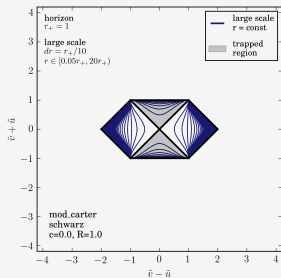
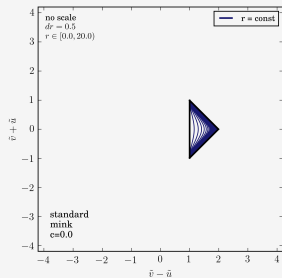
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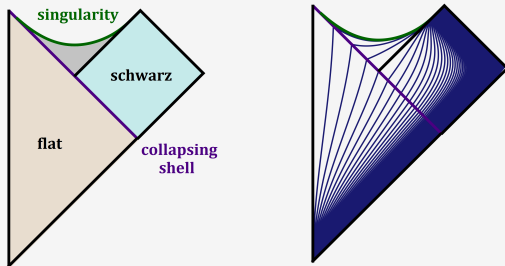


PENROSE DIAGRAMS.



SHELL COLLAPSE.

standard eternal bh from shell collapse



(well-defined piecewise junction yields a matter shell)

Step 4:

Non-Singular Black Holes

SINGULARITY?

singularities:

- ▶ infinite curvature and density ... point mass
- ▶ classical GR breaks down
- ▶ remove w/ curvature cutoff?

removing singularity is restrictive:

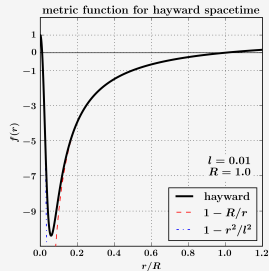
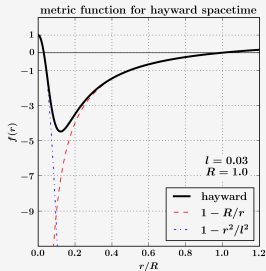
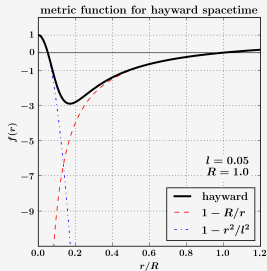
- ▶ $r = 0$ must be timelike (inner horizon forms)
- ▶ for strong spherical symmetry: $f(r) \sim 1 + O(r^2)$ as $r \rightarrow 0$

why?

- ▶ keep curvature finite
- ▶ well-defined cartesian coordinates
- ▶ topological reasons

NON-SINGULAR BH.

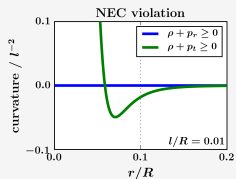
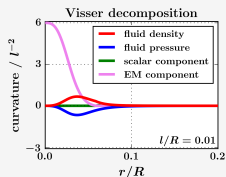
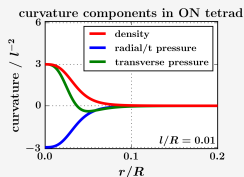
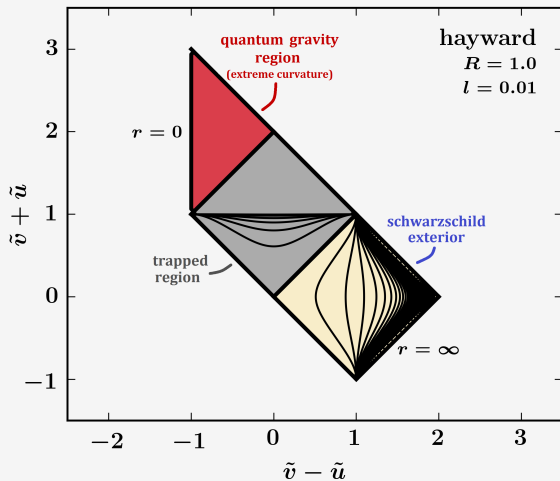
Hayward spacetime: $f(r) = 1 - \frac{Rr^2}{r^3 + Rl^2}$



$$ds^2 = -f(r) dt^2 + f(r) dr^2 + r^2 d\Omega^2$$

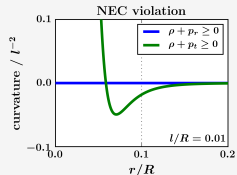
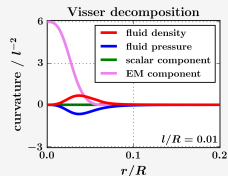
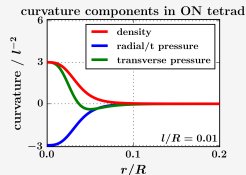
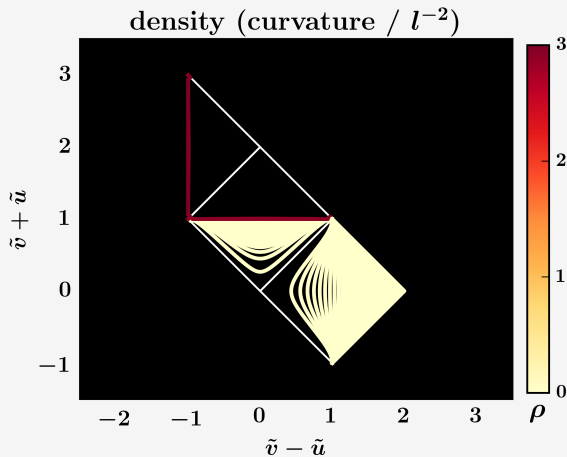
NON-SINGULAR BH.

Hayward spacetime:



NON-SINGULAR BH.

Hayward spacetime:



Step 5:
BH Evaporation

BLACK HOLES RADIATE.

Orders of magnitude for BH evaporation:

mass (M)	radius ($R \propto M$)	temp ($T \propto 1/M$)	lifetime ($t \propto M^3$)
$M_{SMBH} \approx 10^{38}$ kg	1 au	10^{-6} nK	10^{81} GYr
$M_{sun} \approx 10^{30}$ kg	1 km	100 nK	10^{57} GYr
$M_{earth} \approx 10^{24}$ kg	1 mm	100 mK	10^{39} GYr
$M_{yaks} \approx 10^9$ kg	proton	10^{14} K (EWSB)	1000 Yr
$M_{antmegacolony} \approx 10^{5.5}$ kg	tiny	10^{17} K	1 s
$M_{planck} \approx 10^{-8}$ kg	$2 l_p$	10^{30} K (GUT)	10^{-40} s

Simple blackbody spectrum.

EVAPORATION.

evidence for bh evaporation:

- ▶ classical bh thermodynamics

$$dM = \frac{\kappa}{8\pi} dA + \Omega dJ + \Phi dQ$$

- ▶ particle creation derivation
- ▶ euclidean “magic” thermal derivation
- ▶ particle tunneling models
- ▶ vacuum stress tensor derivation
- ▶ and more! (wiki derivation, rindler info derivation, AdS/CFT)

EVAPORATION.

evidence for bh evaporation:

- ▶ classical bh thermodynamics – suggestive

$$dM = \frac{\kappa}{8\pi} dA + \Omega dJ + \Phi dQ$$

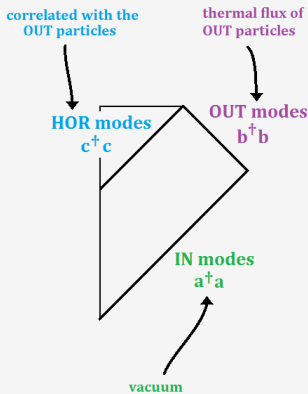
- ▶ particle creation derivation
 - doesn't require bh
- ▶ euclidean “magic” thermal derivation
 - doesn't require bh
- ▶ particle tunneling models
 - negative energy?
- ▶ vacuum stress tensor derivation
 - distinguishes bh from flat space
- ▶ and more! (wiki derivation, rindler info derivation, AdS/CFT)

EVAPORATION.

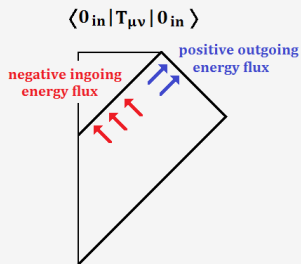
- ▶ many closely intertwined derivations
- ▶ no single, clear, physical picture
(does a clear semiclassical description exist? we think yes)
- ▶ deep relation to entropy

MOST IMPORTANT DYNAMICAL DERIVATIONS.

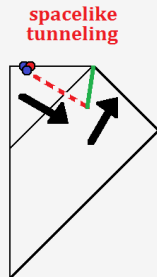
particle creation



vacuum stress tensor

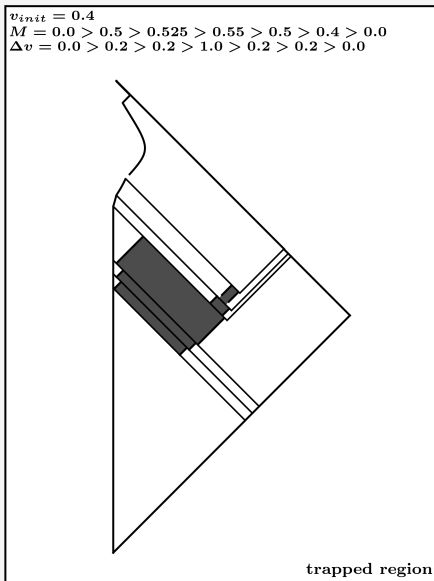


tunneling

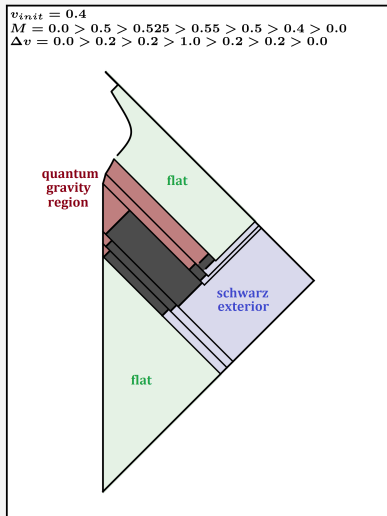
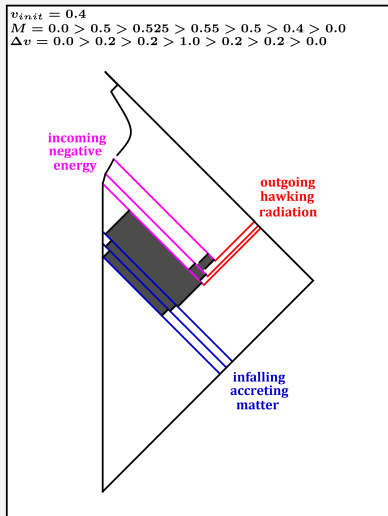


And now for the grand finale...

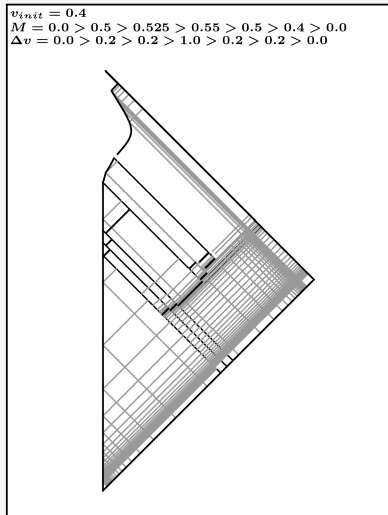
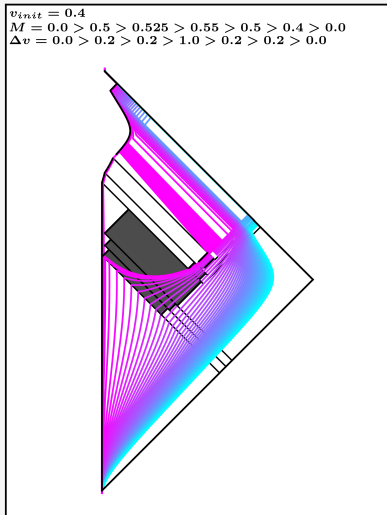
FORMATION AND EVAPORATION.



FORMATION AND EVAPORATION.



FORMATION AND EVAPORATION.



WHAT NOW?

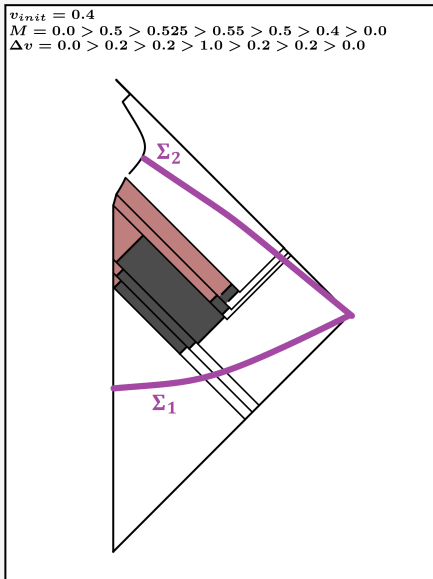
Upcoming papers...

- ▶ algorithm and the new basic diagrams
- ▶ f/e diagrams in asymptotically flat and asymptotically dS space w/ and w/o singularity
- ▶ more after do below

Things to do...

- ▶ put in correct $M(v)$, and extend to dS
- ▶ calculate junction $G^\mu{}_\nu$ and compare to spacelike tunneling
- ▶ repeat Hawking effect derivations in these backgrounds and demonstrate self-consistency
- ▶ rotating regular bh projections?
- ▶ back to roots: entropy, local causal diamond description, stretched horizon description... using new perspectives
- ▶ ...

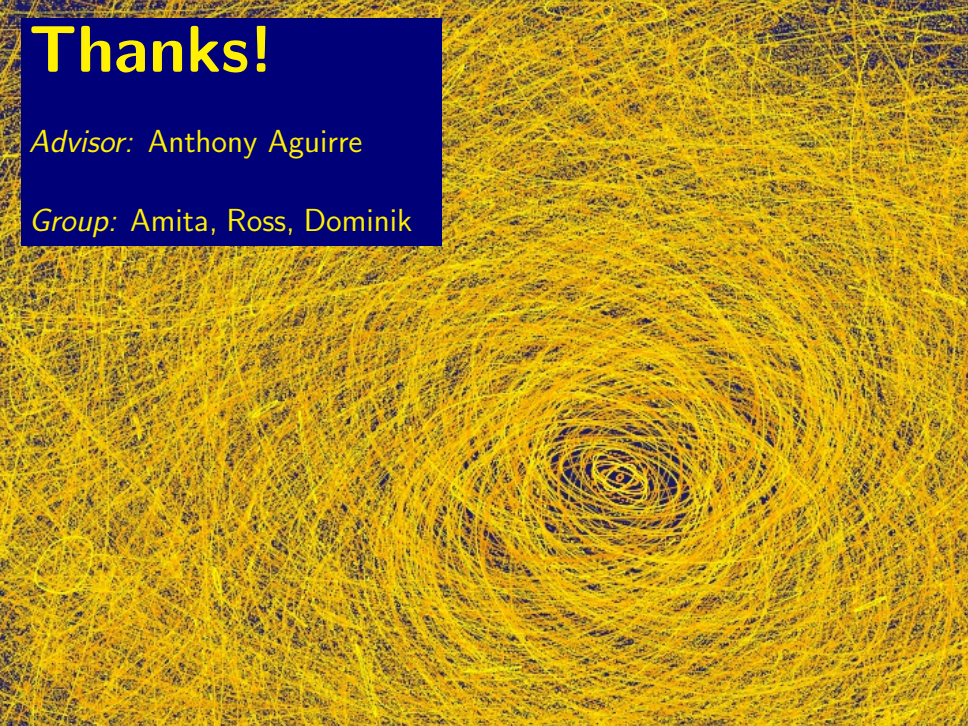
A SENDOFF.



Thanks!

Advisor: Anthony Aguirre

Group: Amita, Ross, Dominik



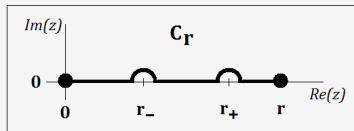
Extra Slides

ALGORITHM.

- ▶ require only that $f(r_0) = 0 \implies f$ analytic at r_0

- ▶ double-null coords from

$$r_*(r) = \int_{C_r} \frac{dz}{f(z)}$$

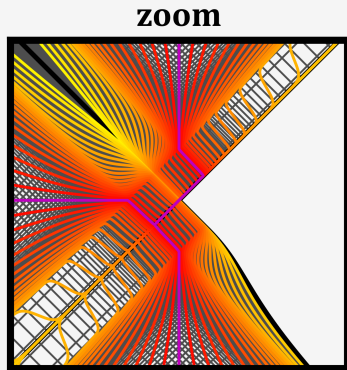
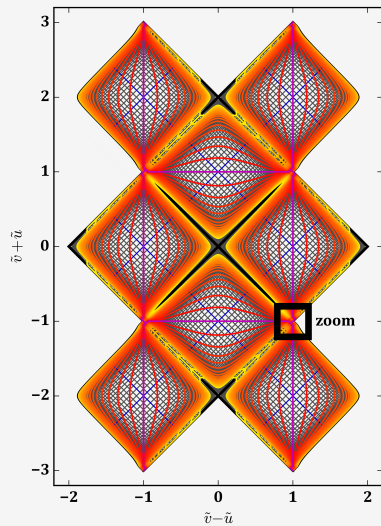


- ▶ target metric is **analytic at horizons**

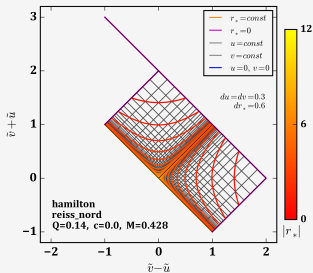
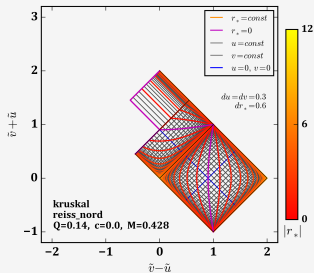
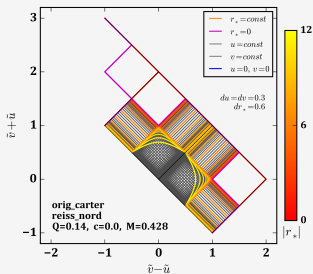
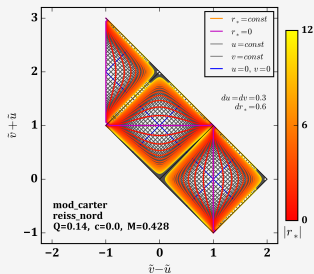
$$ds^2 = - \frac{4\pi^2 |f(r)|}{e^{kr_*(r)}} G_u(u, k) G_v(v, k) d\bar{u}d\bar{v} + r^2 d\Omega^2$$

- ▶ trivially extended to any number of horizons

DETAIL VIEW.

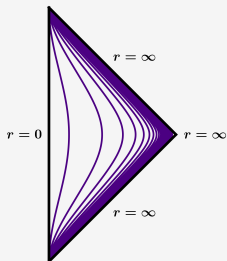


ALTERNATIVE METHODS.

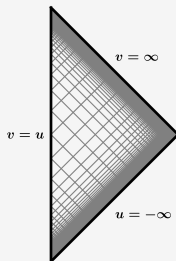


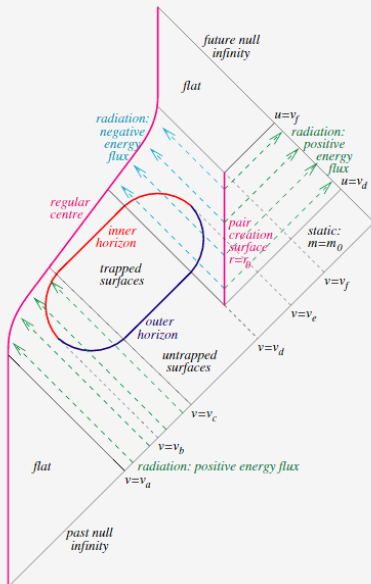
MINKOWSKI SPACE.

lines of
constant radius



lines of
constant u, v





(Hayward 2006)